| Topic | LAUFZE / LAUFPS |
| :--- | :--- |
| Author | Johannes Schweitzer, NORSAR, P.O.Box 53, N-2027 Kjeller <br> Fax: +47 63818719, E-mail: johannes@ norsar.no |
| Version | LAUFZE 6.0 and LAUFPS 3.0 (as of October 2002) |

## User Manual for LAUFZE and LAUFPS

## 1 Introduction

The program LAUFZE calculates travel-time curves for a P- or an S-velocity model. This is a new version of a routine, which was originally developed in the 1970s at the Institute of Geophysics in Karlsruhe, Germany, by the late Prof. Gerhard Müller and Dr. Christoph Gelbke. Since then, the author has extended the code to include many new features and options, in particular for calculating different types of teleseismic phases. The code has been developed at the Institute for Meteorology and Geophysics, University of Frankfurt, Germany, the Institute of Geophysics, Ruhr-University Bochum, Germany, and, most recently, in this new (English) version at NORSAR.

The travel-time curves can be calculated for horizontally layered or spherically symmetric models with or without reduced time scale. The velocity model is defined by input as a function of the depth $z$, the dominant signal period $T_{\text {sig }}$, and the depth-dependent quality factor $Q$ given for a reference period $T_{\text {ref }}$. With this input the program calculates the group velocity as defined by:

$$
u(z, T, Q)=v(z) \cdot\left(1+\frac{1}{\pi \cdot Q(z)} \cdot\left(\ln \left(\frac{T_{\text {ref }}}{T_{s i g}}\right)+1\right)\right)
$$

If no Q -structure is given, the program uses as default value $\mathrm{Q}(\mathrm{z})=10^{6}$. However, Q is always assumed to be frequency independent.

The source can be placed in any depth but the 'receivers' are assumed to be at the Earth's surface. In the case of a spherical Earth model the Earth radius used for the Earth-flattening transformation is 6371 km . However, the Earth's center cannot be reached! The velocities for depths, at which they are not explicitly given, are linearly interpolated.

The whole program is based on the ray approximation of seismic waves, which means that the different kinds of seismic phases must be separately defined by the input parameters. Traveltime curves for the following phase types can be calculated:

I Direct waves from the source to the Earth's surface (only in the case that the source is not at the surface).
II Diving waves from the source radiated down in the Earth.
III Reflections from any layer below the source, back to the Earth's surface (e.g., PcP, $\mathrm{ScP}, \mathrm{PmP}$ ).

IV Reflections of diving waves at any layer back down into the Earth (e.g., PP, SS, PKKP, SKKS).
V Multiples between any two layers (e.g., PPmP, a diving P wave from source to the Earth's surface, reflected from there back into the Earth, and finally reflected at the Mohorovičić (Moho) discontinuity back to the surface).
VI For the phases III - V, any number of multiple reflections can be calculated (e.g., P3, P5KP, SmS3).
VII If the source is not at the surface, for all phases of II - VI the corresponding surface reflections can be calculated (e.g., $\mathrm{pP}, \mathrm{sScS}, \mathrm{pP3KP}$ ).
VIII The multiple reflection(s) as defined under V will automatically be calculated for all above defined phases. That means, e.g., not only for the direct P phase a Moho reverberation PPmP will be calculated but also e.g., for pPKP we will get a pPKPPmP phase.
IX For the direct to the surface radiated wave (see I) reflections can be calculated from any layer between source and the Earth's surface down back into the Earth (e.g., p450P, or smS, but also pP).

All parameters for steering the program must be given in a formatted ASCII file. The program asks for the name of the input file.

All results of the program are written in a ASCII file called laufze-out. This file can then easily be edited and the listed travel-time curves can then be plotted with any plotting routine or used as ASCII input for other programs.

LAUFPS is a program like LAUFZE but it calculates travel times not only for one model ( P or S) but also for both models together in one step, including converted phases.

The newest versions of the programs (including source code, this manual, data files containing examples for input and output files) are located in two compressed tar-files; either in laufze.version.tar.Z or in laufze.version.tar.gz for free download from NORSAR's anonymous ftp-address ftp.norsar.no under the directory /pub/outgoing/johannes/lauf. If using your web-browser, the address is: ftp://ftp.norsar.no/pub/outgoing/johannes/lauf. Questions related to program updates and maintenance should be directed to the author.

## 2 Getting Started

This section describes how the example for LAUFZE can be started and executed. The simplest way to use the program for own travel-time calculations is to use the following examples and to modify the input data and parameters for your need. The meaning and format of the input is described in the following sections.

## Installation of LAUFZE:

1) Make a sub-directory for LAUFZE, copy the compressed tar-file containing the laufzesoftware package from the ftp.norsar.no site, decompress it, and run:

You will then have a directory containing the following files and subdirectories:
bin/ bin_l/ examples/ man/ README src/
The file README contains a complete list of all files included in the laufze-software package and a short explanation of these files.
2) If needed, recompile the software in the $\mathrm{src} /$ subdirectory by running:
make -f Makefile.laufze
and/or
make -f Makefile.laufps
The software was tested under UNIX as well under LINUX and should therefore run on both platforms without any compatibility problems. In the case of a LINUX system please use the corresponding Makefiles with the extension _linux.

## 3) Executing LAUFZE:

Change to the subdirectory examples/.
Here you will find an example for an input file.
LAUFZE runs with one input file. To check your installation, try the following:

```
run:
../bin/laufze
```

The program needs one input file in ASCII format. You will be asked for the name of the input file and you here answer with laufze-in. This file contains all parameters to steer the travel-time calculations and the layered velocity model. All results of the program are written in a file called laufze-out. The output file you get should be identical to the file laufze-out.test distributed with the laufze-software package. Contents and structure of these files will be explained in the following sections.

The program LAUFPS uses the same input file format as LAUFZE but it needs two files, one containing the P -velocity model and ray definitions for P phases and one file containing the $S$-velocity model and ray definitions for $S$ phases. After starting the program with

## ../bin/laufps

you will be asked for names of the files containing the P - and S -velocity models and the file to steer the behaviour of all P-to-SV and/or SV-to-P conversions (e.g., laufp-dat, laufs-dat, and laufps-in). If you use the files as delivered with the laufze-software package, the LAUFPS output file laufps-out should be identical to the file laufps-out.test.

## 3 The File laufze-in

The file laufze-in must contain the velocity model for P (or S ) waves and all information about the seismic phases for which travel times shall be calculated. The program asks for the name of the file containing this information in the format below described. The user can of course use any file name.
example for a laufze-in file

```
For a source in 100 km, Jeffreys-Bullen Model
            0.000 180.000 0.00 0 0
            0.000 0.000 0 0.0
        0.0 6.11 STRU 0.000 ! for pP
        33.0 6.11
        33.0 7.76
    100. 7.95 SOUR
    200. 8.26
    300. 8.58
    413. 8.97
    600. 10.25
    800. 11.00
    1000. 11.42
    1200. 11.71
    1400. 11.99
    1600. 12.26
    1800. 12.53
    2000. 12.79
    2200. 13.03
    2400. 13.27
    2600. 13.50
    2800. 13.64
    2898. 13.64 REFL ! for PCP
    2898. 8.10
    3000. 8.22
    3200. 8.47
    3400. 8.76
    3600. 9.04
    3800. 9.28
    4000. 9.51
    4200. 9.70
    4400. 9.88
    4600. 10.06
    4800. 10.25
    4982. 10.44
    5121. 10.44 REFL ! for PKiKP
    5121. 11.16
    5700. 11.26
                                    ! blank line, more layers
        1 1 20
            1 1 ! for PP
        1 2 ! for P3
        21 1 ! for PKKP
        21 2 ! for P3KP
        ! blank line: no more such mult. phases
        ! for PcPPcP + PKiKPPKiKP
        ! blank line: no more such mult. phases
        ----- end of the example
```

The contents of the laufze-in file is as follows:

1. 1 line of maximum 80 characters with any explaining text as TITLE.
2. 1 line in FORMAT (3F10.3,3I5) containing the parameters: RMIN, RMAX, VR, IELAS, NF11.

RMIN is the beginning of the distance range from which onset times are calculated. Either measured in [deg] or in [km], see the definition of VR.

RMAX as RMIN but the end of the distance range used to print out the travel-time branches.

VR is the velocity or slowness to reduce the travel times.
If VR $>0$, RMIN and RMAX are measured in $[\mathrm{km}]$ and $\mathbf{V R}$ is a reduction velocity [km/s].
If $\mathbf{V R}<=0, \mathbf{R M I N}$ and RMAX are measured in [deg] and VR is a reduction slowness [s/deg].

IELAS if this flag is set to $1, \mathrm{Q}(\mathrm{z})$ is set to $10^{6}$ in all depths (pure elastic case).
NF11 if this flag is set to 1 , no direct up-going rays from a source below the surface are calculated.
3. 1 line in FORMAT (2F10.3,3I5) containing the parameters: PER, PEREFF, LA1, LA2, NLA.

PER is the dominant signal period $\mathrm{T}_{\text {sig }}[\mathrm{s}]$.
PERREF is the reference period $\mathrm{T}_{\text {ref }}[\mathrm{s}]$.
If these two period values are set to 0 s , the default value of 1 s is used.
LA1 is the number of the upper layer for the described reverberations (see V of the program options in the introduction).

LA2 as LA1, now the number of the lower layer.
NLA gives the number of reverberations.
The multiple travels through the depth range $\mathbf{Z}(\mathbf{L A} 1)<=\mathbf{Z}(\mathrm{I})<\mathbf{Z}(\mathbf{L A} 2)$ NLA times more than the regular phase. If LA1 $=\mathbf{L A} \mathbf{2}$ or NLA $=0$, no reverberations are calculated.
4. Now follows the model. The model is defined by one line for each depth with velocity information. All lines must fit in the FORMAT (2F10.3,A4,6x,F10.3) and contain the parameters $\mathbf{Z}, \mathbf{V}, \mathbf{A Z}, \mathbf{Q U}$. The model can contain a maximum of 1000 layers. First order discontinuities for one of the given parameters has to be defined by 2 lines in the same depth $\mathbf{Z}$.
$\mathbf{Z}$ depth in [km] below the Earth's surface. The surface has the depth $\mathbf{Z}(1)=0$.
V seismic velocity in the depth $\mathbf{Z}$.

AZ four characters long key words, with which one can define special actions in this depth:
$=$ SOUR means that the source is in this depth of the model.
= SURF means that the source is in this depth and that for all (!) phases also the surface reflections are calculated (e.g., $\mathrm{pP}, \mathrm{sScS}, \ldots$...).
$=$ STRU means that an up-going direct ray is reflected in this depth back down into the Earth (see IX of the program options in the introduction). If STRU is set at the surface, the classical surface reflection is calculated (i.e., only pP or sS but not e.g., pPP or sScS).
= REFL means that steep-angle reflections from this depth are calculated (see III of the program options in the introduction).
In all other cases $\mathbf{A Z}$ must be blank.
QU is the quality factor for seismic waves in this depth; if $\mathrm{QU}=0$. the program sets it by default to $\mathrm{QU}=1000000$.

An empty line finishes the model input.
5. 1 line in FORMAT (3I5) with the three parameters IS, IA, IB.

IS $=0$ the input model is assumed to be flat, i.e., it consists of a set of horizontally flat layers.
$=1$ the input model is spherical and has to be transformed by the Earth-flattening transformation.

IA $=\mathrm{I}$; only the parts of the travel-time curves, which have their turning points below the I'th layer, are calculated. If IA $=1$, all travel-time branches of all phases are calculated.

IB gives the number of rays, which will have their turning points between two depth points of the model; IB values of $10-20$ usually give a good approximation of the travel-time branch.
6. In the following line(s), the reflections of diving rays at any layer back down into the Earth can be defined (see IV of the program options in the introduction). For each (!) such reflection 1 line in FORMAT (2I10) is needed with the parameters IKMG and MULT. If no (further) reflections of this type are to be calculated, one has to give a blank line.

IKMG is the number of the layer at which the ray is reflected; e.g., for PP one has to set $\mathbf{I K M G}=1$.

MULT gives the number of reflections at this reflector (e.g., for PP, SS, or PKKP one has to set MULT = 1, for P3, S3, or S3KS one has to use MULT =2).
7. Finally, multiple reflections for the steep-angle reflections as defined with $\mathbf{A Z}=$ REFL can be ordered with the following line(s) in FORMAT (I10) containing the parameter MULTR. No (further) multiples of this type have to be indicated by another blank line.

MULTR gives the number of multiples for each order steep-angle reflection.
MULTR = 1 will, for example, result in PmP2 or ScS2 and MULT $=2$ will give, e.g., ScS3.

## 4 The File laufze-out

With the above example for a laufze-in file, you will obtain the output-file laufze-out. Please note that the output file has been truncated by numerous lines to reduce the number of pages in this manual. The ASCII listing of the travel times can easily be extracted and the user can plot them with any plotting program after some simple editing work. The original output file has 3117 lines and is included in the laufze-software package. Explanations are included in [ .... ]:

```
                                    example for a laufze-out file
Travel times from LAUFZE 6.0
For a source in 100 km, Jeffreys-Bullen Model
Distance range
RMIN = 0.000 deg
RMAX = 180.000 deg
Ray parameter to reduce travel times P = 0.000 s/deg
The travel times are calculated for a group velocity
at a reference period of 1.000 s
Model input (depth, velocity)
+ modified velocity-depth function after application
    of the Earth-flattening transformation
```

| Z | V ( Z ) | Q ( Z ) | $U(Z, Q, P E R)$ | AZ ( Z ) | FLATT EARTH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | [ Z-FL | $\mathrm{U}-\mathrm{FL}]$ |
| 0.000 | 6.110 | 1000000.0 | 6.110 | STRU | 0.000 | 6.110 |
| 33.000 | 6.110 | 1000000.0 | 6.110 |  | 33.086 | 6.142 |
| 33.000 | 7.760 | 1000000.0 | 7.760 |  | 33.086 | 7.800 |
| 100.000 | 7.950 | 1000000.0 | 7.950 | SOUR | 100.793 | 8.077 |
| 200.000 | 8.260 | 1000000.0 | 8.260 |  | 203.207 | 8.528 |
| 300.000 | 8.580 | 1000000.0 | 8.580 |  | 307.293 | 9.004 |
| 413.000 | 8.970 | 1000000.0 | 8.970 |  | 426.995 | 9.592 |
| 600.000 | 10.250 | 1000000.0 | 10.250 |  | 630.162 | 11.316 |
| 800.000 | 11.000 | 1000000.0 | 11.000 |  | 854.873 | 12.580 |
| 1000.000 | 11.420 | 1000000.0 | 11.420 |  | 1087.799 | 13.546 |
| 1200.000 | 11.710 | 1000000.0 | 11.710 |  | 1329.566 | 14.427 |
| 1400.000 | 11.990 | 1000000.0 | 11.990 |  | 1580.871 | 15.367 |
| 1600.000 | 12.260 | 1000000.0 | 12.260 |  | 1842.496 | 16.372 |
| 1800.000 | 12.530 | 1000000.0 | 12.530 |  | 2115.328 | 17.464 |
| 2000.000 | 12.790 | 1000000.0 | 12.790 |  | 2400.367 | 18.642 |
| 2200.000 | 13.030 | 1000000.0 | 13.030 |  | 2698.760 | 19.903 |
| 2400.000 | 13.270 | 1000000.0 | 13.270 |  | 3011.817 | 21.290 |


| 2600.000 | 13.500 | 1000000.0 | 13.500 |  | 3341.056 | 22.808 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 2800.000 | 13.640 | 1000000.0 | 13.640 |  | 3688.241 | 24.335 |
| 2898.000 | 13.640 | 1000000.0 | 13.640 | REFL | 3865.526 | 25.022 |
| 2898.000 | 8.100 | 1000000.0 | 8.100 |  | 3865.526 | 14.859 |
| 3000.000 | 8.220 | 1000000.0 | 8.220 |  | 4055.441 | 15.535 |
| 3200.000 | 8.470 | 1000000.0 | 8.470 |  | 4445.107 | 17.017 |
| 3400.000 | 8.760 | 1000000.0 | 8.760 |  | 4860.167 | 18.785 |
| 3600.000 | 9.040 | 1000000.0 | 9.040 |  | 5304.164 | 20.785 |
| 3800.000 | 9.280 | 1000000.0 | 9.280 |  | 5781.437 | 22.996 |
| 4000.000 | 9.510 | 1000000.0 | 9.510 |  | 6297.381 | 25.554 |
| 4200.000 | 9.700 | 1000000.0 | 9.700 |  | 6858.818 | 28.466 |
| 4400.000 | 9.880 | 1000000.0 | 9.880 |  | 7474.555 | 31.936 |
| 4600.000 | 10.060 | 1000000.0 | 10.060 |  | 8156.231 | 36.190 |
| 4800.000 | 10.250 | 1000000.0 | 10.250 |  | 8919.681 | 41.568 |
| 4982.000 | 10.440 | 1000000.0 | 10.440 |  | 9704.131 | 47.886 |
| 5121.000 | 10.440 | 1000000.0 | 10.440 | REFL 10375.893 | 53.211 |  |
| 5121.000 | 11.160 | 1000000.0 | 11.160 |  | 10375.893 | 56.880 |
| 5700.000 | 11.260 | 1000000.0 | 11.260 |  | 14339.481 | 106.911 |
|  |  |  |  |  |  |  |
| Travel-time branch | 1 and all the following ones were calculated, |  |  |  |  |  |

P H A S E :
[ If NF11 is set to 1 , this wave will not be calculated ]
Directly upgoing wave
[ DELTA is the distance measured in [km] or in [deg], see input parameter VR, TT is the (eventually reduced) travel time, AIN is the radiation angle at the source, $\mathrm{T}^{*}$ is the travel time divided by the mean quality factor TT/Q, ATT is the amplitude attenuation due to $\mathrm{T}^{*}$, i.e., $\operatorname{ATT}=\operatorname{EXP}\left(-2 * \mathrm{PI}^{*} \mathrm{f}_{\mathrm{ref}} * \mathrm{~T}^{*}\right]$, and P is the ray parameter measured in [s/deg] ]

| DELTA | TT | AIN | T* | ATT | P |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| 0.000 | 13.931 | 180.000 | 0.000 | 1.000 | 0.000 |
| 0.033 | 13.940 | 177.722 | 0.000 | 1.000 | 0.547 |
| 0.066 | 13.967 | 175.443 | 0.000 | 1.000 | 1.094 |
| 0.099 | 14.012 | 173.165 | 0.000 | 1.000 | 1.639 |
| 0.132 | 14.075 | 170.886 | 0.000 | 1.000 | 2.181 |
| 0.166 | 14.158 | 168.608 | 0.000 | 1.000 | 2.719 |
| 0.200 | 14.260 | 166.329 | 0.000 | 1.000 | 3.254 |
| 0.234 | 14.381 | 164.051 | 0.000 | 1.000 | 3.783 |
| 0.269 | 14.524 | 161.772 | 0.000 | 1.000 | 4.306 |
| 0.305 | 14.688 | 159.494 | 0.000 | 1.000 | 4.823 |
| 0.342 | 14.874 | 157.215 | 0.000 | 1.000 | 5.332 |
| 0.380 | 15.085 | 154.937 | 0.000 | 1.000 | 5.832 |
| 0.419 | 15.321 | 152.658 | 0.000 | 1.000 | 6.323 |
| 0.459 | 15.584 | 150.380 | 0.000 | 1.000 | 6.804 |
| 0.500 | 15.877 | 148.101 | 0.000 | 1.000 | 7.275 |
| 0.543 | 16.201 | 145.823 | 0.000 | 1.000 | 7.734 |
| 0.588 | 16.559 | 143.544 | 0.000 | 1.000 | 8.181 |
| 0.635 | 16.954 | 141.266 | 0.000 | 1.000 | 8.614 |
| 0.685 | 17.389 | 138.987 | 0.000 | 1.000 | 9.034 |
| 0.737 | 17.870 | 136.709 | 0.000 | 1.000 | 9.440 |

## Program Description

| 0.792 | 18.401 | 134.430 | 0.000 | 1.000 | 9.831 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| 0.850 | 18.988 | 132.152 | 0.000 | 1.000 | 10.207 |
| 0.913 | 19.638 | 129.873 | 0.000 | 1.000 | 10.566 |
| 0.980 | 20.359 | 127.595 | 0.000 | 1.000 | 10.908 |
| 1.053 | 21.162 | 125.316 | 0.000 | 1.000 | 11.234 |
| 1.131 | 22.059 | 123.038 | 0.000 | 1.000 | 11.541 |
| 1.218 | 23.067 | 120.759 | 0.000 | 1.000 | 11.830 |
| 1.313 | 24.204 | 118.481 | 0.000 | 1.000 | 12.101 |
| 1.418 | 25.494 | 116.203 | 0.000 | 1.000 | 12.353 |
| 1.536 | 26.969 | 113.924 | 0.000 | 1.000 | 12.584 |
| 1.670 | 28.667 | 111.646 | 0.000 | 1.000 | 12.796 |
| 1.823 | 30.640 | 109.367 | 0.000 | 1.000 | 12.988 |
| 2.000 | 32.953 | 107.089 | 0.000 | 1.000 | 13.159 |
| 2.207 | 35.688 | 104.810 | 0.000 | 1.000 | 13.310 |
| 2.451 | 38.953 | 102.532 | 0.000 | 1.000 | 13.439 |
| 2.742 | 42.881 | 100.253 | 0.000 | 1.000 | 13.547 |
| 3.091 | 47.631 | 97.975 | 0.000 | 1.000 | 13.634 |
| 3.512 | 53.386 | 95.696 | 0.000 | 1.000 | 13.699 |
| 4.018 | 60.330 | 93.418 | 0.000 | 1.000 | 13.743 |
| 4.621 | 68.624 | 91.139 | 0.000 | 1.000 | 13.765 |

P H A S E:

## Diving wave

[ DELTA is the distance measured in [km] or in [deg], see input parameter VR, TT is the (eventually reduced) travel time, AIN is the radiation angle at the source, $\mathrm{T}^{*}$ is the travel time divided by the mean quality factor TT/Q, ATT is the amplitude attenuation due to $\mathrm{T}^{*}$, i.e., $\mathrm{ATT}=\operatorname{EXP}\left(-2 * \mathrm{PI}^{*} \mathrm{f}_{\mathrm{ref}} * \mathrm{~T}^{*}\right], \mathrm{P}$ is the ray parameter measured in [s/deg], and for diving waves also the depth [km] of the ray's turning point is given. ]

| DELTA | TT | AIN | T* | ATT | PS |  |
| ---: | ---: | ---: | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |
| 4.961 | 73.311 | 90.000 | 0.000 | 1.000 | 13.767 | 100.000 |
| 6.323 | 92.033 | 85.613 | 0.000 | 1.000 | 13.727 | 105.303 |
| 6.995 | 101.248 | 83.803 | 0.000 | 1.000 | 13.687 | 110.602 |
| 7.549 | 108.820 | 82.420 | 0.000 | 1.000 | 13.647 | 115.897 |
| 8.040 | 115.504 | 81.258 | 0.000 | 1.000 | 13.607 | 121.186 |
| 8.488 | 121.598 | 80.238 | 0.000 | 1.000 | 13.568 | 126.472 |
| 8.906 | 127.257 | 79.319 | 0.000 | 1.000 | 13.529 | 131.753 |
| 9.299 | 132.574 | 78.477 | 0.000 | 1.000 | 13.490 | 137.029 |
| 9.673 | 137.613 | 77.696 | 0.000 | 1.000 | 13.451 | 142.301 |
| 10.031 | 142.418 | 76.966 | 0.000 | 1.000 | 13.413 | 147.569 |
| 10.375 | 147.021 | 76.277 | 0.000 | 1.000 | 13.374 | 152.832 |
| 10.706 | 151.448 | 75.624 | 0.000 | 1.000 | 13.336 | 158.091 |
| 11.027 | 155.720 | 75.003 | 0.000 | 1.000 | 13.298 | 163.345 |
| 11.338 | 159.853 | 74.409 | 0.000 | 0.999 | 13.261 | 168.595 |
| 11.641 | 163.860 | 73.840 | 0.000 | 0.999 | 13.223 | 173.840 |
| 11.936 | 167.752 | 73.292 | 0.000 | 0.999 | 13.186 | 179.081 |
| 12.223 | 171.539 | 72.765 | 0.000 | 0.999 | 13.149 | 184.317 |
| 12.504 | 175.230 | 72.255 | 0.000 | 0.999 | 13.112 | 189.549 |
| 12.779 | 178.832 | 71.762 | 0.000 | 0.999 | 13.076 | 194.777 |
| 13.049 | 182.351 | 71.284 | 0.000 | 0.999 | 13.039 | 200.000 |

[ Each layer of the model gives one block of rays (number as given as IB) and forms one 'branch' of the traveltime curve. These rays are always written as one block in the listing. Here all blocks with rays bottoming in the mantle were omitted! ]
[ The next possible rays are the phases bottoming in the Earth's core: here PKPab, PKPbc ]

| 178.309 | 1310.499 | 18.832 | 0.001 | 0.996 | 4.444 | 3959.714 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 173.109 | 1287.400 | 18.810 | 0.001 | 0.996 | 4.439 | 3961.852 |

[ All the bottoming in the outer core rays were deleted!]

```
154.616 1186.983 8.731 0.001 0.996 2.090 5121.000
```

[ The inner core boundary (ICB) is a first order discontinuity with a positive velocity jump. The following rays 'bottoming' in the boundary build the over-critical part of the travel-time curve of PKiKP, the reflection from the ICB! ]

| 154.616 | 1186.983 | 8.731 | 0.001 | 0.996 | 2.090 | 5121.000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 144.603 | 1166.084 | 8.699 | 0.001 | 0.996 | 2.082 | 5121.000 |
| 140.610 | 1157.784 | 8.667 | 0.001 | 0.996 | 2.075 | 5121.000 |
| 137.605 | 1151.561 | 8.636 | 0.001 | 0.996 | 2.067 | 5121.000 |
| 135.111 | 1146.414 | 8.605 | 0.001 | 0.996 | 2.060 | 5121.000 |
| 132.943 | 1141.955 | 8.574 | 0.001 | 0.996 | 2.052 | 5121.000 |
| 131.006 | 1137.987 | 8.543 | 0.001 | 0.996 | 2.045 | 5121.000 |
| 129.244 | 1134.390 | 8.513 | 0.001 | 0.996 | 2.038 | 5121.000 |
| 127.621 | 1131.087 | 8.482 | 0.001 | 0.996 | 2.031 | 5121.000 |
| 126.111 | 1128.026 | 8.452 | 0.001 | 0.996 | 2.024 | 5121.000 |
| 124.695 | 1125.167 | 8.423 | 0.001 | 0.996 | 2.017 | 5121.000 |
| 123.361 | 1122.481 | 8.393 | 0.001 | 0.996 | 2.009 | 5121.000 |
| 122.096 | 1119.944 | 8.364 | 0.001 | 0.996 | 2.002 | 5121.000 |
| 120.893 | 1117.538 | 8.334 | 0.001 | 0.996 | 1.996 | 5121.000 |
| 119.744 | 1115.249 | 8.305 | 0.001 | 0.997 | 1.989 | 5121.000 |
| 118.644 | 1113.065 | 8.277 | 0.001 | 0.997 | 1.982 | 5121.000 |
| 117.587 | 1110.975 | 8.248 | 0.001 | 0.997 | 1.975 | 5121.000 |
| 116.571 | 1108.971 | 8.220 | 0.001 | 0.997 | 1.968 | 5121.000 |
| 115.590 | 1107.044 | 8.191 | 0.001 | 0.997 | 1.962 | 5121.000 |
| 114.643 | 1105.190 | 8.163 | 0.001 | 0.997 | 1.955 | 5121.000 |

[ Now followed the deleted PKPdf branch. ]

Surface reflection of the direct wave
[ See the parameters STRU and/or SURF in the input file. The ray output for pP , pPKP , and pPKiKP (overcritical part) was deleted. ]

```
        P H A S E :
Diving wave 1-times reflected at the Earth's surface
```

[ See the parameters IKMG and MULT in the input file. The ray output for PP, P'P', and PKiKP2 (over-critical part) was deleted. ]

```
        P H A S E :
Diving wave 2-times reflected at the Earth's surface
```

[ See the parameters IKMG and MULT in the input file. The ray output for P3, P'3, and PKiKP3 (over-critical part) was deleted. ]

```
        P H A S E :
Diving wave 1-times reflected down at layer 21
```

[ See the parameters IKMG and MULT in the input file; layer 21 is here the core-mantle boundary. The ray output for PKKP and PKiKKiKP (over-critical part) was deleted. ]

```
    P H A S E :
Diving wave 2-times reflected down at layer 21
```

[ See the parameters IKMG and MULT in the input file; layer 21 is here the core-mantle boundary (CMB). The ray output for P3KP and P3KiKP (over-critical part) was deleted. ]

```
    P H A S E :
Steep-angle reflection from 2898.000 km
```

[ See the parameter $\mathbf{A Z}=\mathbf{R E F L}$ in the input file. Steep-angle reflection (i.e., below the critical point) from the CMB ; the ray output for PcP was deleted. ]

```
    P H A S E :
Steep-angle reflection from 5121.000 km
```

[ See the parameter AZ = REFL in the input file. Steep-angle reflection (i.e., below the critical point) from the ICB; the ray output for PKiKP was deleted. ]

```
            P H A S E :
Multiple reflection ( 1-times) for the
    Steep-angle reflection from 2898.000 km
```

[ See the parameters AZ = REFL and MULTR in the input file. Multiple steep-angle reflection (i.e., below the critical point) from the CMB; the ray output for PcP2 was deleted. ]

```
        P H A S E :
Multiple reflection ( 1-times) for the
    Steep-angle reflection from 5121.000 km
```

[ See the parameters AZ = REFL and MULTR in the input file. Multiple steep-angle reflection (i.e., below the critical point) from the ICB; the ray output for PKiKP2 was deleted. ]

## 5 The Program LAUFPS and the File laufps-in

The program LAUFPS calculates travel-time curves for a given velocity model, as does the program LAUFZE, and was developed on the base of LAUFZE. In addition to LAUFZE, LAUFPS calculates P- and S-phase travel-time curves in one step and it can also calculate travel-time curves for converted phases. Therefore, the input for LAUFPS consists of two files: one containing the P-velocity model and one containing the S-velocity model. Both files must have the same format as the input files to run LAUFZE, e.g., one file is then called laufp-dat and one is called laufs-dat. Both files must sample the velocity models (i.e., the P and the S models) identically and the source must be at the same depth. However, these input files can be extended at three points to inform the program in the case of multiple phases, how often these reverberations are eventually travelling through the model as converted phase. These additions are the following ones (I refer to the number of the format description of the input-file for LAUFZE):
3. 1 line in FORMAT (2F10.3,4I5) containing the parameters: PER, PEREFF, LA1, LA2, NLA.

PER is the dominating signal period $\mathrm{T}_{\text {sig }}[\mathrm{s}]$.
PERREF is the reference period $\mathrm{T}_{\text {ref }}[\mathrm{s}]$.
If these two period values are set to 0 s , the default value of 1 s is used.
LA1 is the number of the upper layer for the described reverberations (see V of the program options in the introduction).

LA2 as LA1, now the number of the lower layer.
NLA gives the number of reverberations.
The multiples travel through the depth range $\mathbf{Z}(\mathbf{L A 1})<=\mathbf{Z}(\mathrm{I})<\mathbf{Z}(\mathbf{L A} 2)$
NLA times more than the regular phase. If LA1 $=\mathbf{L A} \mathbf{2}$ or NLA $=0$, no reverberations are calculated.

NLA2 gives how many of the NLA reverberations are travelling as converted phase (NLA2 must be <= NLA).
6. In the following line(s) the reflections of diving rays at any layer back down into the Earth can be defined (see IV of the program options in the introduction). For each (!) such reflection 1 line in FORMAT (3I10) is needed with the parameters IKMG, MULT, and MULT2. If no (further) reflections of this type shall be calculated one has to give a blank line.

IKMG is the number of the layer at which the ray is reflected; e.g., for PP one has to set $\mathbf{I K M G}=1$.

MULT gives the number of reflections at this reflector (e.g., for PP, SS, or PKKP one has to set MULT = 1, for P3, S3, or S3KS one has to use MULT =2).

MULT2 gives how many of the MULT reverberations are travelling as a converted phase (MULT2 must be <= MULT), e.g., the travel-time curve of PPS will need to set $\mathbf{I K M G}=1, \mathbf{M U L T}=2$, and MULT2 $=1$.
8. Finally, multiple reflections for the steep-angle reflections as defined with $\mathbf{A Z}=$ REFL, can be ordered with the following line(s) in FORMAT (2I10) containing the parameter MULTR and MULTR2. No (further) multiples of this type have to be indicated by another blank line.

MULTR give the number of multiples for each order steep-angle reflection. MULTR $=1$ will e.g., result in PmP2 or ScS2 and MULT $=2$ will give e.g., ScS3.

MULTR2 gives how many of the MULTR reverberations are travelling as converted phase (MULTR2 must be <= MULTR), e.g., the travel-time curve of PcPScS will need to set MULTR $=2$, and MULTR2 $=1$.

The directory examples/ contains files with one P- (laufp-dat) and one S-velocity model (laufs-dat) with some of the mentioned settings. In addition to these input files, the program LAUFPS needs one file containing steering parameters for each travel-time curve to define further conversions. This file (here e.g., called laufps-in) must contain the following information in the described format:
a) In the first line the parameter KONSOR in FORMAT (I5). KONSOR steers the general behaviour of LAUFPS:
$=0 ;$ no conversions are calculated (not even the ones defined above!).
$=1$; only conversions from P to SV type phases are calculated.
$=2$; only conversions from SV to P type phases are calculated.
$=3$; all types of conversions are calculated.
b) For each (!) phase, as calculated after setting KONSOR $=0$ and listed in laufps-out with a own phase header, one has to add one line with the parameters KON, KON1, NDISK1, KON2, NDISK2 in FORMAT (5I5).

KON $=0$; no conversion for this phase.
$=1$; this is a P phase and we get a P to SV conversion.
$=2$; this is an $S$ phase and we get a $S V$ to $P$ conversion.
$=9$; the next entry is for the same phase but another conversion type.

KON1 = 1 ; the first conversion happens on the ray path down.
$=2$; the first conversion happens on the ray path up.
NDISK1 gives the number of the discontinuity for the first conversion: see listing in a table in the laufps-out file.

KON2 $=1$; an possible second conversion happens on the ray path down.
$=2$; an possible second conversion happens on the ray path up.
NDISK2 gives the number of the discontinuity for the second conversion.

```
-------------------example for a laufps-in file
00003
    0 0 0 0 0 0 Pdirect -->
    0}00000000 Sdirect --> >>>
    1 2 3 0 0 0 0 P/PKP --> PKS
    1 2 2 0 0 0 P/PKP --> P/PKP at Moho to SV
    0 pP -->
    0 PP -->
    0 PPS -->
    0 S/SKS -->
    0 sS -->
    S- SS -->
    2 3 S3KP -->
    2 3 PCP --> PcS
    PCPSCS -->
    ScS --> ScP
    2 3
```

The output from program LAUFPS can become very complex and long. However, the principle listing looks very like the output for LAUFZE and I have added no example of an output file here. For an example of a laufps-out file applying the here listed laufps-in file, please see the files in the directory examples/.

